Autonomous Vehicle Simulation (AVS) Laboratory, University of Colorado

Basilisk Technical Memorandum

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WEIGHT LEAST-SQUARES MINIMUM-NORM COARSE SUN HEADING ESTIMATOR

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Status: Released
Scope/Contents
This is a report documenting the results of the unit test performed for the coarse sun sensor sun point vector estimation algorithm. A weighted least-squares minimum-norm algorithm is used to estimate the body-relative sun heading using a cluster of coarse sun sensors. Using two successive sun heading evaluation the module also computes the inertial angular velocity vector. As rotations about the sun-heading vector are not observable, this angular velocity vector only contains body rates orthogonal to this sun heading vector.

Rev	Change Description	By	Date
1.0	Initial Documentation	S. Piggott	2016-10-01
1.1	Modified Format to BSK documentation	H. Schaub	2018-04-29

1.2	Added User Guide Section	H. Schaub	2018-04-29
1.3	Added discussion on the inertial angular velocity vector evaluation	H. Schaub	2018-05-26
1.4	Added residuals and links for FSW Review	T. Teil	2019-02-12

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1 Introduction

When in safe mode, the spacecraft uses its coarse sun sensors (CSSs) in order to point the vehicle's solar arrays at the Sun. This is done in order to ensure that the vehicle gets to a power-positive state with a minimum set of sensors in order to recover from whatever event triggered the transition to safe mode. The nominal vehicle considered in this report has 8 coarse sun sensor (CSS) sensors available to it which allows it to resolve the exact sun direction in almost all body axes as long as all sensors are functional. With these cosine CSS a minimum of 3 sensor must provide a signal to determine a unique answer.

1.1 Sun Heading Evaluation

If more than 3 CSS detect a sun signal, the algorithm needs to be able to obtain the sun pointing vector that best fits the current outputs from all of the CSSs. This is done by a least squares estimation process that provides the sun vector that best fits from a weighted least squares perspective. The weights are simply set based on the current output of each sensor which ensures that the sensors that have the best measurements are trusted the most. If 3 CCS see the sun, then a unique heading is computed. If 1-2 CSS see the sun then a minimum norm solution is evaluated. If no CSS sees the sun then a zero vector is returned. The details of this algorithm are available in Steve O'Keefe's PhD dissertation. *

The algorithm stores its internal variables in the CSSWLSConfig data structure with the input message provides the CSS sensor values. The output is a `NavAttIntMsg` message that contains the estimated sun-heading vector in body frame components. This sun-heading estimation algorithm does not use any information stored from previous frames so it is a fresh computation every time it is called. It can therefore be called at any rate needed by the system.

* O'Keefe Public Dissertation Link

1.2 Partial Angular Velocity Evaluation

Using two successive sun-heading vector evaluations it is possible to evaluate a partial solution of the spacecraft inertial angular velocity vector. Note that rate about the sun heading vector are not obsdervable, but rates about the other two axes can be obtained.

Let $\boldsymbol{d}_n$ be current sun heading vector from the above sun heading algorithm. The prior estimate is denoted as $\boldsymbol{d}_{n-1}$, while Δt is the time step between the two measurements. The angular velocity vector is then evaluated using

$$\boldsymbol{\omega}_{B/N} = \frac{\boldsymbol{d}_n \times \boldsymbol{d}_{n-1}}{|\boldsymbol{d}_n \times \boldsymbol{d}_{n-1}|} \arccos\left(\frac{\boldsymbol{d}_n \cdot \boldsymbol{d}_{n-1}}{|\boldsymbol{d}_n||\boldsymbol{d}_{n-1}|}\right) \frac{1}{\Delta t} \tag{1}$$

These vector evaluations are performed using $\mathcal{B}$ frame vector components.

Note that iff both $\boldsymbol{d}_n$ and $\boldsymbol{d}_{n-1}$ are nearly collinear a zero body rate vector is returned. Further, during start-up and reset operations it is possible that Δt might be zero for a single evaluation. In this case also a zero rate vector is returned.

1.3 Post-Fit residuals

In order to get a measurement of filter performance, post-fit residuals are computed in the method `computeWlsResiduals`.

This method takes in the current coarse-sun sensor measurements, as well as the best estimate and compares the two. This is done by doting the estimate with all the normals of activated sensors, and subtracting them to the actual measured value.

$$r_i = \boldsymbol{n}_i \cdot \boldsymbol{d} - \boldsymbol{n}_i \cdot \hat{\boldsymbol{d}} \tag{2}$$

Equations in 2 show the process for the i-th sensor, where $\boldsymbol{d}$ is the true value, and $\hat{\boldsymbol{d}}$ is the filter estimate. These residuals are then output in the Sunline-FSW message.

2 Test Design

The unit test for the cssWlsEst module is located in:

`fswAlgorithms/attDetermination/CSSEst/_UnitTest/CSSWlsEstUnitTest.py`

Please see the python script for information on test setup and initial conditions.

This unit test is designed to functionally test the algorithm outputs as well as get complete code path coverage. The test design is broken up into four main parts:

1. Main Body Axis Estimates: The principal body axes (b1, b2, b3) are tested with both positive and negative values to ensure that all axes are correctly estimated.
2. Double Coverage Test: There are small regions of pointing where only two sun sensors provide "good" values, which results in a case where only the minimum norm solution can be used instead of a full least squares solution. One of these regions is tested here.
3. Single Coverage Test: One of the sensors used for the double coverage test is zeroed in order to simulate a sensor failure and hit the single coverage code. The accuracy of this estimate is severely compromised.
4. Zero Coverage Case: The case where no sensors provide an above-threshold value is tested here.

3 Test Results

The values obtained in the test over time are best visualized in Figure 1. That shows a comparison between the Sun pointing vector input to the test and the estimate provided by the algorithm.

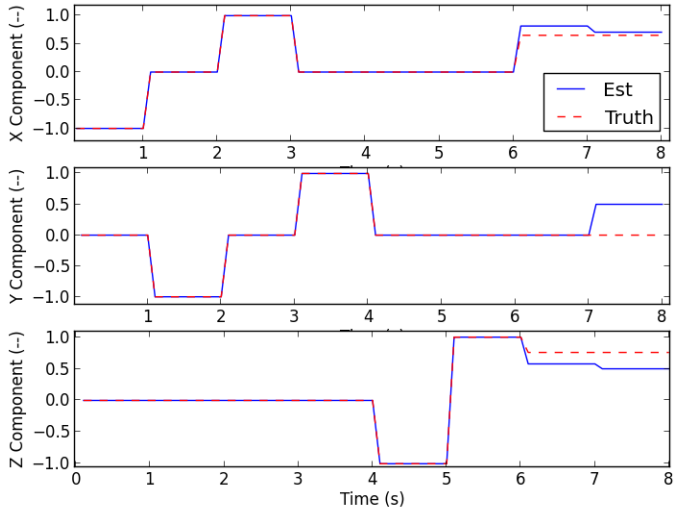

Fig. 1: Truth and Estimated Sun Pointing Vector

As this plot shows, the algorithm is very accurate up until 6.0 seconds, so both directions of the three primary body axes are estimated precisely. Then the double coverage case is reasonably accurate, but no longer precise as there isn't sufficient information available to get a good pointing direction. The single coverage test is not accurate at all (45 degrees of error), but that is simply the best that the algorithm can do with that limited information.

Figure 2 shows the number of CSSs used by the algorithm to estimate the sun pointing vector over the duration of the test. It continues for longer than Figure 1 because the algorithm stops setting its output message once it gets to the zero valid sensors case as there is no good information to provide.

1. Main Body Axis Estimates: The sun pointing estimation algorithm is not required to provide a precise estimate of the Sun direction. This algorithm is only intended to be used in safe mode where the arrays only need to be approximately pointed at the Sun. For this reason, a pointing vector was flagged as successful when it provided the Sun direction within 17.5 degrees which corresponds to a cosine loss of approximately 5%. All body axes met this criteria with large margins. A check was also performed that verified that the predicted number of CSSs matched up with what the algorithm used and this check was also 100% successful. The UseWeights flag was initially set to False, and then was changed to True after two cases to ensure that the algorithm works correctly in both cases. Test successful.

2. Double Coverage Test: The same accuracy criteria was used for this test. This is mostly a function of CSS geometry and it is also the main driving case for the success criteria used. It was correct to within 14 degrees. The predicted number of CSSs used (2) also matched the algorithm's selection. Test successful.

3. Single Coverage Test: The single coverage case did not have its accuracy tested as there are no accuracy requirements for this case. It simply must provide an estimate and exit. The predicted number of CSSs used (1) did match the algorithm's selection. Test successful.

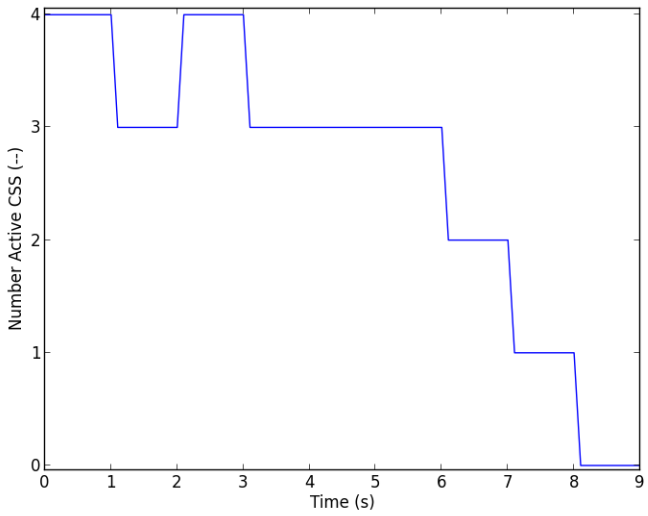

Fig. 2: Number of CSSs Used in Estimate

4. Zero Coverage Test: The zero coverage test is only provided here to demonstrate that the algorithm passivates its outputs without hitting any unacceptable event. It does correctly flag that no valid CSSs were found during the test. Test successful.

5. Angular Velocity Test: The same 8 unit CSS configuration is used as in the earlier tests, but the true sun heading is set equal to $\hat{\boldsymbol{b}}_1$. A BSK sample time of 0.5 seconds is setup, and the simulation is run 3 times to reach a simulation time of 1.0 seconds. It takes 2 steps for the module to evaluate the update rate $\mathrm{d}t$, thus the expected rate estimate is a zero vector for these steps. As the sun heading is being evaluated in the 2nd step, with the 3rd step there is a non-zero $\mathrm{d}t$ value, but the old and new sun-heading vectors are the same. The expected rate output is again a zero vector. Next the true sun heading is changed to be $\hat{\boldsymbol{b}}_2$, corresponding to a $90\mathrm{deg}$ heading change about $\hat{\boldsymbol{b}}_3$. The simulation is run for two more steps. The expected inertial body rate with step 4 would be $-\pi$ rad/sec about $\hat{\boldsymbol{b}}_3$. The 5th step must yield again a zero rate vector as the sun heading has not changed. Next, a reset function is called and a single simulation step is called. The expected output is the zero rate vector again. Finally, the true sun heading vector is changed back to $\hat{\boldsymbol{b}}_1$ and another simulation step is performed to show a $+\pi$ rad/sec rotation about $\hat{\boldsymbol{b}}_3$. The test results status is: PASSED

4 Test Coverage

The method coverage for all of the methods included in the cssWlsEst module are tabulated in Table 2

Table 2: ADCS Coarse Sun Sensor Estimation Coverage Results

Method Name	Unit Test Coverage (%)	Runtime Self (%)	Runtime Children (%)
SelfInit_cssWlsEst	100.0	0.0	0.0
CrossInit_cssWlsEst	100.0	0.0	0.0
computeWlsmn	100.0	0.01	0.64
Update_cssWlsEst	100.0	0.04	0.88

For all of the code this test was designed for, the coverage percentage is 100%. For Safe Mode, we do expect this algorithm to be the highest usage element from an ADCS perspective, so the CPU usage is almost certainly fine as is. The main penalty comes from the use of matrix multiply in the

computeWlsmn function. The only issue of note here is that the matrix multiply algorithm(s) use in the FSW should be optimized as much as possible as they are major sources of CPU spin.

5 Conclusions

The safe mode sun vector estimator described in this document is functionally ready from a PDR perspective. It has no noted failure cases, all code is tested for statement coverage, and it successfully meets its test criteria for all cases. The only area where there might be a question is the desired behavior for zero-coverage cases. We may wish to change the outputs to something more obviously in-error instead of just having the algorithm go silent.

6 User Guide

6.1 Input/Output Messages

The module has 1 required input messages, and 1 output message:

- `navStateOutMsgName` – This output message, of type `NavAttIntMsg`, provides the attitude navigation message containing the estimated sun heading vector `vehSunPntBdy`, as well as the partially observed body rate vector `omega_BN_B`.
- `cssDataInMsgName` – This input message, of type `CSSArraySensorIntMsg`, receives the CSS sensor message

6.2 Module Parameters and States

The module has the following parameter that can be configured:

- `useWeights` – Flag indicating whether or not to use weights for least squares. Default value is 0, indicating not to use the weights.
- `sensorUseThresh` – This double contains the minimum sensor signal to consider. The default value is zero.
- `CSSData` – [REQUIRED] Array of `CSSConfigFswMsg` messages that contain the CSS sensor states.